



Neutrino Physics: an Introduction

Lecture 2: Neutrino mixing and oscillations

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Lecture 1: Neutrino detection and basic properties

- Unique properties
- Discovery of neutrino flavours
- Measuring mass, helicity, interactions

Lecture 2: Neutrino mixing and oscillations

- Solar and atmospheric puzzles and solutions
- Neutrino mixing, oscillations, flavour conversions
- The three-neutrino mixing picture

Lecture 3: Neutrinos in astrophysics and cosmology

- Low-energy (meV) cosmological neutrinos
- Medium-energy (MeV) supernova neutrinos
- High-energy ($> \text{TeV}$) astrophysical neutrinos

Neutrino Physics: an Introduction (Lecture 2)

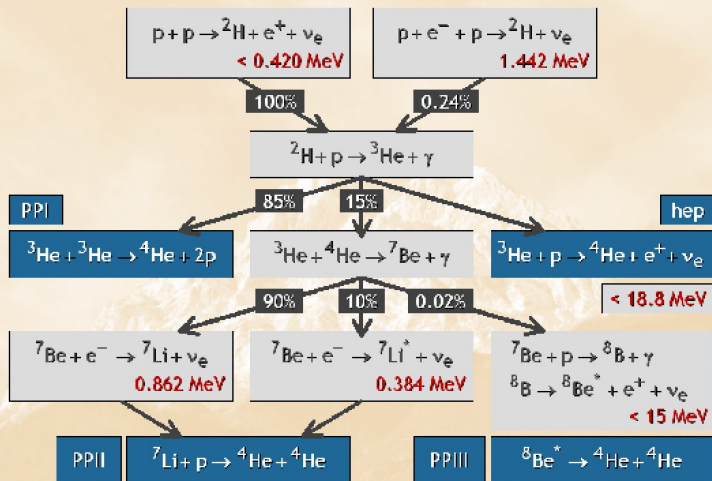
- 1 Solar and atmospheric neutrino puzzles
- 2 Atmospheric ν solution: mixing and vacuum oscillations
- 3 The path to the solution for solar ν puzzle
- 4 The three-neutrino mixing picture

Neutrino Physics: an Introduction (Lecture 2)

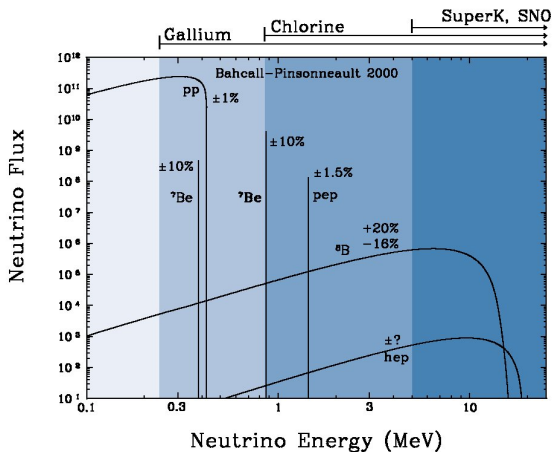
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Neutrinos from the Sun

Hydrogen burning: Proton-Proton Chains



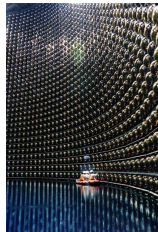
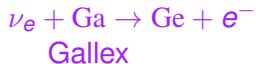
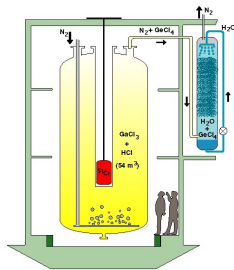
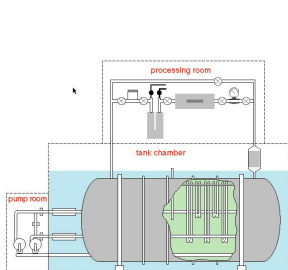
The solar neutrino spectra



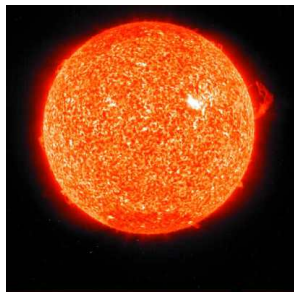
- Magnitudes of fluxes depend on details of solar interior
- Spectral shapes robustly known

Detecting neutrinos from the Sun

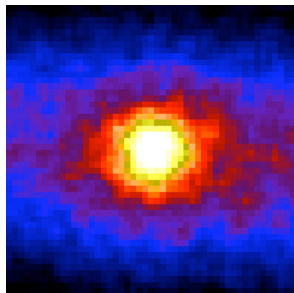
- The Sun produces ν_e
- These ν_e can be detected at Earth: difficult, but possible



Seeing the Sun with neutrinos



- Light from the Sun's surface:
due to nuclear reactions
millions of years ago
- Neutrinos from the Sun's core:
due to nuclear reactions
8 minutes ago

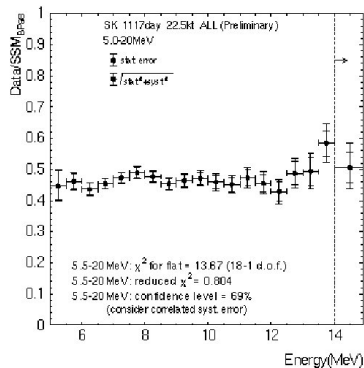
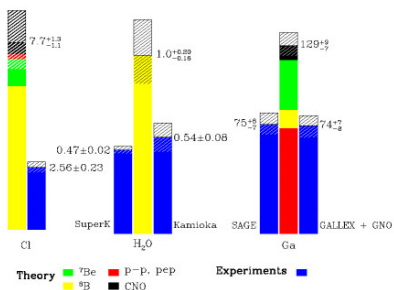


- We know how much light we get from the Sun...
- So we know how many neutrinos should arrive.

BUT...

Do we really understand how the Sun shines ?

Total Rates: Standard Model vs. Experiment
Bahcall-Pinsonneault 2000



The solar neutrino puzzle

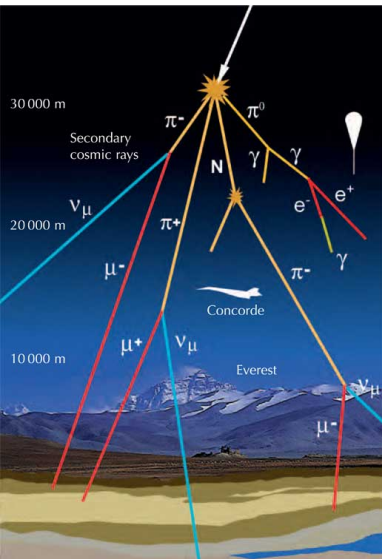
- Only about 30%–50% of neutrinos from the Sun found
- Different experiments give different neutrino loss...
(They look at different energy ranges, of course..)
- SuperKamiokande shows similar neutrino loss at all energies

Possible resolutions of the puzzle

- The astrophysicists cannot calculate accurately
- The experimentalists cannot measure accurately
- Neutrinos behave differently from what everyone thought !

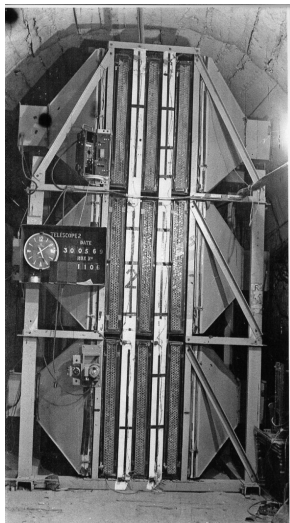
.... remained unresolved for about 40 years !

Neutrino production from cosmic rays



- $\pi^+ \rightarrow \mu^+ + \nu_\mu$
- $\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$

The first “atmospheric” neutrinos detected in India



Detector in
Kolar Gold Fields

DETECTION OF MUONS PRODUCED BY COSMIC RAY NEUTRINO DEEP UNDERGROUND

C. V. ACHAR, M. G. K. MENON, V. S. NARASIMHAM, P. V. RAMANA MURTHY
and B. V. SREEKANTAN,

Tata Institute of Fundamental Research, Colaba, Bombay

K. HINOTANI and S. MIYAKE,
Osaka City University, Osaka, Japan

D. R. CREED, J. L. OSBORNE, J. B. M. PATTISON and A. W. WOLFENDALE
University of Durham, Durham, U.K.

Received 12 July 1965

Physics Letters 18, (1965) 196
(15th Aug 1965)

EVIDENCE FOR HIGH-ENERGY COSMIC-RAY NEUTRINO INTERACTIONS*

F. Reines, M. F. Crouch, T. L. Jenkins, W. R. Kropp, H. S. Gurr, and G. R. Smith

Case Institute of Technology, Cleveland, Ohio

and

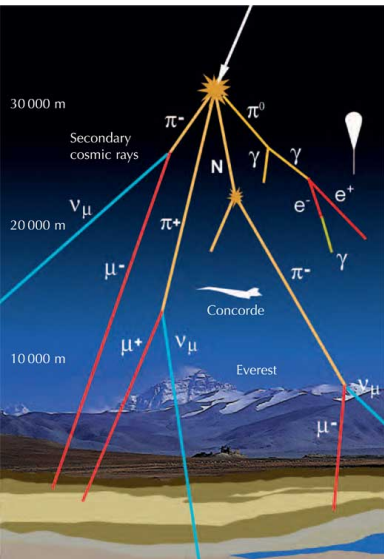
J. P. F. Sellschop and B. Meyer

University of the Witwatersrand, Johannesburg, Republic of South Africa

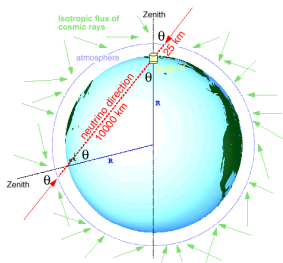
(Received 26 July 1965)

PRL 15, (1965) 429
(30th Aug 1965)

Neutrino production from cosmic rays

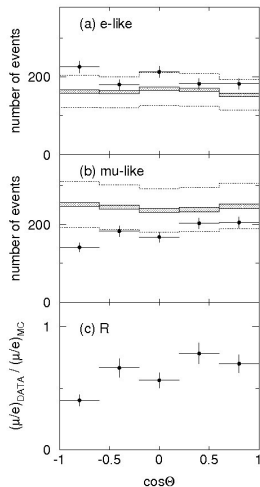


- $\pi^+ \rightarrow \mu^+ + \nu_\mu$
- $\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$
- “ ν_μ ” flux = $2 \times$ “ ν_e ” flux
- “Down” flux = “Up” flux



Atmospheric neutrino puzzle

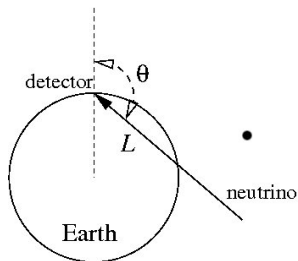
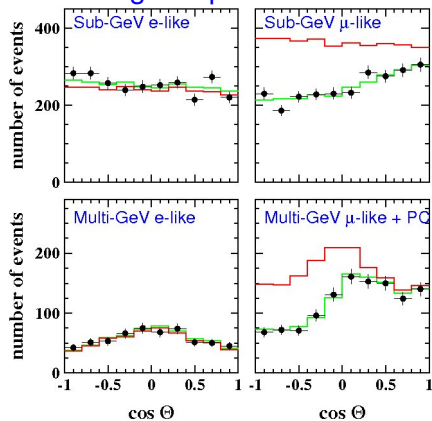
Double ratio:



- Expected $R = 1$
- Observed $R < 1$

Atmospheric neutrino puzzle

Zenith angle dependence:



Super-Kamiokande

Preliminary observations from zenith angle data

- Electron neutrinos match predictions
- High energy ν_μ from above: match predictions
- High energy ν_μ through the earth: partially lost
- Low energy ν_μ : lost even when coming from above, loss while passing through the Earth even greater

Where are we now

- About 20 years ago: in the middle of two long-standing puzzles

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The breakthrough idea



Bruno Pontecorvo

(original idea suggested for solar neutrinos,
with neutrino-antineutrino mixing.)

Бруно Понтекорво

Maybe the neutrino flavours change !

- All the experiments are looking for ν_e and ν_μ
- What if ν_e / ν_μ are getting converted to ν_τ ?
- This is possible, but only if the neutrinos have different masses and they mix !

What is meant by neutrino mixing ?

Neutrino flavours ν_e, ν_μ, ν_τ do not have fixed masses !!

For example, ν_e - ν_μ mixing:



$$\nu_2 = -\nu_e \sin \theta + \nu_\mu \cos \theta$$



$$\nu_1 = \nu_e \cos \theta + \nu_\mu \sin \theta$$

$\cos^2 \theta$

$\sin^2 \theta$

- Only ν_1 and ν_2 have fixed masses
(*They are eigenstates of energy / eigenstates of evolution*)
- Then, if you produce ν_e , it may be observed as ν_μ !

Effective Hamiltonian for a single neutrino

$$H = \sqrt{p^2 + m^2} \approx p + \frac{m^2}{2p} \approx p + \frac{m^2}{2E}$$

Schrödinger's equation:

$$i \frac{d}{dt} |\nu(t)\rangle = H |\nu(t)\rangle$$

Time evolution:

$$\begin{aligned} |\nu(t)\rangle &= |\nu(0)\rangle e^{-iHt} \\ &= |\nu(0)\rangle e^{-ipt} e^{-i\frac{m^2}{2E}t} \end{aligned}$$

- Simple for a mass eigenstate with fixed momentum !

Time evolution for a flavour eigenstate

- Initial flavour state $|\nu_\alpha\rangle$:

$$|\nu_\alpha\rangle = \cos\theta|\nu_1\rangle + \sin\theta|\nu_2\rangle$$

- State after time t :

$$|\nu_\alpha(t)\rangle = \cos\theta|\nu_1\rangle e^{-ipt} e^{-i\frac{m_1^2}{2E}t} + \sin\theta|\nu_2\rangle e^{-ipt} e^{-i\frac{m_2^2}{2E}t}$$

- “Survival” probability of finding the flavour $|\nu_\alpha\rangle$ at time t :

$$P(\nu_\alpha \rightarrow \nu_\alpha) = |\langle\nu_\alpha|\nu_\alpha(t)\rangle|^2$$

Vacuum oscillations

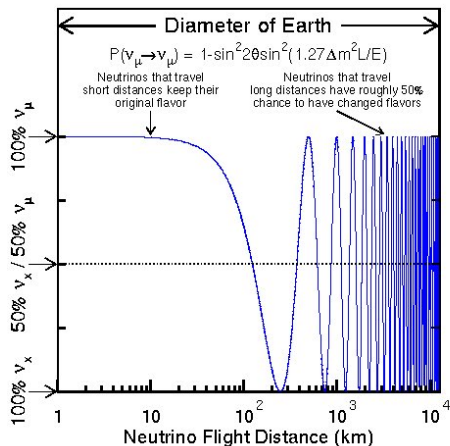
$$P(\nu_\alpha \rightarrow \nu_\alpha) = 1 - \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$$

$$\Delta m^2 \equiv m_2^2 - m_1^2$$

(In Natural units, where $c = 1 = \hbar$)

Amplitude, wavelength:

Neutrino oscillations as a function of distance travelled



- More neutrinos 'lost' when $\cos(\Theta) < 0$

(Θ : angle made with the zenith)

$$P(\nu_\alpha \rightarrow \nu_\alpha) = 1 - \sin^2 2\theta \sin^2 \left(1.27 \frac{\Delta m^2 (\text{eV}^2) L (\text{km})}{E (\text{GeV})} \right)$$

Broad features of atmospheric ν data explained

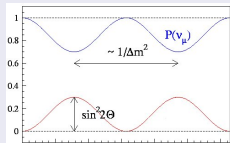
- Electron neutrinos match predictions
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Atmospheric ν solution through “vacuum oscillations”

Prerequisites

- Neutrino flavours mix with each other
- Neutrinos have different masses
- ν_e do not participate in the oscillations

Neutrino oscillations: ν_μ oscillate into ν_τ



$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$$

$$\Delta m^2 \equiv m_2^2 - m_1^2$$

- Measurements can determine $\sin^2 2\theta_{\text{atm}}$ and Δm_{atm}^2 .

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The breakthrough idea



Bruno Pontecorvo

Original idea with $\nu - \bar{\nu}$ mixing

Бруно Понтекорво

Maybe the neutrino flavours change !

- All the experiments are looking for ν_e
- What if ν_e are getting converted to other flavours of neutrinos (ν_μ or ν_τ) ?
- This is possible, but only if the neutrinos have different masses and they mix !

Neutrino flavour changes inside the Sun

John
Bahcall



Lincoln
Wolfenstein



Stanislav
Mikheyev

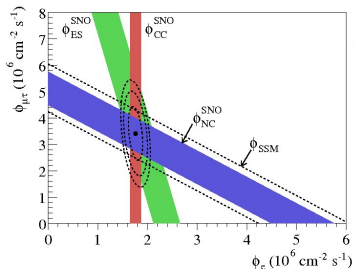
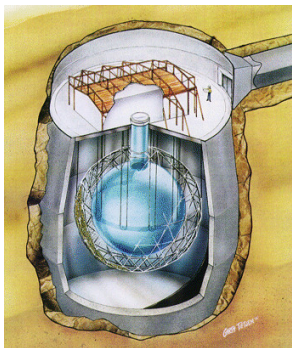


Alexei
Smirnov



- **Bahcall:** Calculated the neutrino production inside the Sun in detail
- **Wolfenstein:** Showed that the neutrino mixing gets affected by the matter inside the Sun
- **Mikheyev – Smirnov:** Showed how these matter effects affect the neutrino flavour changes

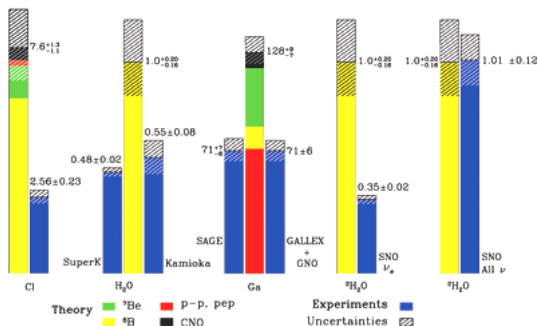
Heavy water Cherenkov experiment: SNO



- Heavy water Cherenkov
- $\nu_e D \rightarrow p p e^-$
sensitive to Φ_e
- $\nu_{e,\mu,\tau} e^- \rightarrow \nu_{e,\mu,\tau} e^-$
Sensitive to $\Phi_e + \Phi_{\mu\tau}/6$
- $\nu_{e,\mu,\tau} D \rightarrow n p \nu_{e,\mu,\tau}$
sensitive to $\Phi_e + \Phi_{\mu\tau}$
- Neutral current: no effect of oscillations

Solar neutrino problem settled (2002)

Total Rates: Standard Model vs. Experiment
Bahcall-Pinsonneault 2000



- All neutrinos from the Sun are now accounted for !
- Our understanding of the Sun is vindicated...

Solution of solar neutrino problem

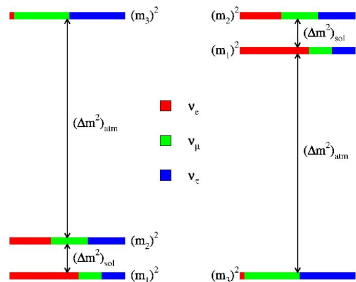
- ν_e mixes with ν_μ/ν_τ
- Survival probability is almost flat:
no oscillations observable but “flavour conversions”
- The measurements can determine $\sin^2 \theta_\odot$
- To determine Δm_\odot^2 accurately, have to conduct terrestrial experiments (using reactors)

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Three-neutrino mixing and open questions

Mixing of $\nu_e, \nu_\mu, \nu_\tau \Rightarrow \nu_1, \nu_2, \nu_3$ (mass eigenstates)



- $\Delta m_{\text{atm}}^2 \approx 2.4 \times 10^{-3} \text{ eV}^2$
- $\Delta m_{\odot}^2 \approx 7.5 \times 10^{-5} \text{ eV}^2$
- $\theta_{\text{atm}} \approx 45^\circ$
- $\theta_{\odot} \approx 32^\circ$
- $\theta_{\text{reactor}} \approx 9^\circ$

- Mass ordering: Normal or Inverted ?
- What are the absolute neutrino masses ?
- Are there more than 3 neutrinos ?
- Is there leptonic CP violation ?
- Can neutrinos be their own antiparticles ?

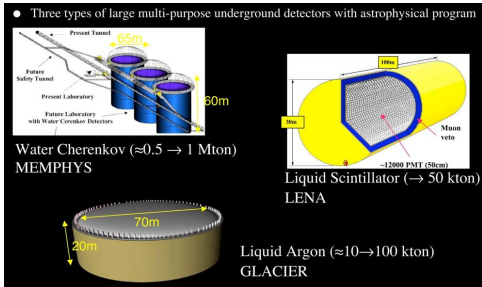
And how do neutrinos get their mass at all ?

- In Standard Model of particle physics, the mass arises from the interaction between a left-handed particle, a right-handed particle, and Higgs.

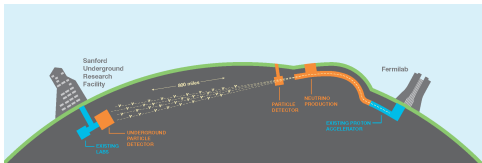
For example, e_L , e_R and h come together to give mass to the electron, which contains both e_L and e_R .

- But there is no right-handed neutrino !
⇒ Higgs mechanism is not enough
- There *has to be* something beyond the Standard Model, perhaps even beyond our current imagination.

Bigger detectors, ambitious experiments



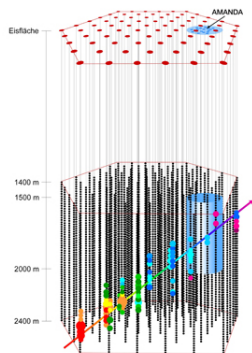
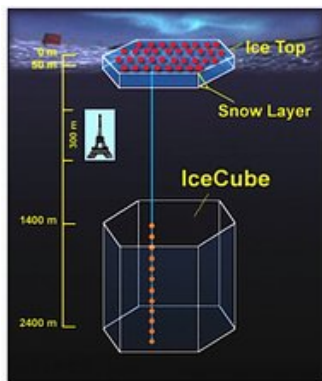
- Megaton water Cherenkov detectors
- 50 kiloton scintillator detectors
- 100 kiloton liquid Ar detectors



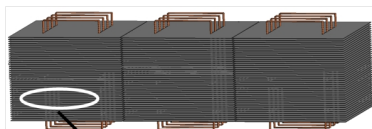
- Deep Underground Neutrino Experiment (DUNE)
- Detector 1600 km away from source

Below the antarctic ice: Gigaton IceCube

1 000 000 000 000 litres of ice



Coming soon inside a mountain near you: INO



5.6 cm thick iron plate

4 cm air gap for RPC detector

India-based Neutrino Observatory

- In a tunnel below a peak (Bodi West Hills, near Madurai)
- 1 km rock coverage from all sides
- 50 kiloton of magnetized iron (50 000 000 kg)
- **Can distinguish neutrinos from antineutrinos**
- Determining mass hierarchy from atmospheric neutrinos

Where are we now (end of Lecture 2)

- Atmospheric neutrino problem solved through neutrino mixing and vacuum oscillations
- Solar neutrino problem solved through neutrino mixing, and modification of vacuum mixing due to matter
- Determination of three-neutrino parameters one of the main goals of worldwide experiments